

Part A: Forms of quadratic functions

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Use the area model to convert between forms.

	Factored form	Area Model	Standard Form
1.	$(x + 4)(x + 8)$		$x^2 + 12x + 32$
2.	$(x + 7)(x + 10)$		$x^2 + 17x + 70$
3.	$(-2x + 6)(4x - 7)$		$-8x^2 + 38x - 42$
4.	$(x + 6)(x - 6)$		$x^2 - 36$
5.	$(2x + 6)(x + 2)$ OR $(x + 3)(2x + 4)$		$2x^2 + 10x + 12$

2 EACH:

1: AREA MODEL

1: ANSWER

6. What is the standard form of $y = (3x - 4)^2$?

a. $y = 9x^2 + 16$

b. $y = 9x^2 - 24x + 16$

c. $y = 9x^2 - 16$

d. $y = 9x^2 + 8x + 16$

(2)

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Part B: Critical features of parabolas

7. Which one of the parabolas opens down?

- a. $y = (x - 4)(x + 5)$
- b. $y = (2x - 9)(3x - 5)$
- c. $y = (3x + 4)(-4x - 1)$
- d. $y = (x + 2)(x - 1)$

[2]

8. What are the x -intercepts of the parabola given by: $y = (x - 2)(3x + 4)$

- a. 2 and 0
- b. 1 and 3
- c. 2 and $-\frac{4}{3}$
- d. 2 and $\frac{4}{3}$

[2]

9. What is the y -intercept of the parabola given by: $y = x^2 + 5x - 2$

- a. -3
- b. -2
- c. 1
- d. 5

[2]

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Part C: Solving quadratic equations

10. Solve the equation below for x . Then, check your solutions using substitution. Show your work.

Solve: $x^2 - x - 12 = 0$

	x	3
x	x^2	$3x$
-4	$-4x$	-12

$$(x+3)(x-4) = 0$$

$$x+3=0$$

$$x = -3$$

[3] $\left\{ \begin{array}{l} \frac{1}{2}: \text{ATTEMPT TO FACTOR} \\ \frac{1}{2}: \text{CORRECT FCT'd FORM} \\ 1: 2 \text{ EQNS.} \\ 1: 2 \text{ SOLUTIONS} \end{array} \right.$

$$x - 4 = 0$$

$$x = 4$$

Check solution #1:

$$x^2 - x - 12 = 0$$

Check solution #2:

$$x^2 - x - 12 = 0$$

[2] $\left\{ \begin{array}{l} 1: \text{SUBSTITUTES EACH SOLUTION SEPERATELY} \\ 1: 0=0 \text{ FOR BOTH CHECKS.} \end{array} \right.$

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Part D: Conceptual writing

Answer **ONLY ONE** of the questions below.

Check the box to the left of the question that you want to be graded.

Check here
to grade
question 11

11. A student was given the following equation in factored form:

$$y = (x - 4)(x + 8)$$

- a. Will the vertex of this parabola be a maximum or a minimum point? MINIMUM
b. Explain your answer using complete sentences.

BOTH SLOPES ARE POSITIVE [1]
SO THE PARABOLA OPENS UP [1]
SO THE VERTEX IS A MINIMUM. [1]

Check here
to grade
question 12

12. Explain your process for factoring $f(x) = x^2 + 3x - 10$

[2]: EXPLAIN PROCESS

Give two more examples of *different* quadratic functions in standard form where your process would also work.

1. (e.g.) $x^2 + 3x + 2$

[1/2] EACH: FACTORABLE
OVER \mathbb{Z}

2. $x^2 + 6x + 7$

Part E: Real-world problems

13. A cannon fires a cannonball off of a cliff into the ocean. The ball's height h , in meters, above the ocean is a function of time t in seconds, as shown in the following equation:

$$h(t) = -5t^2 + 20t + 25$$

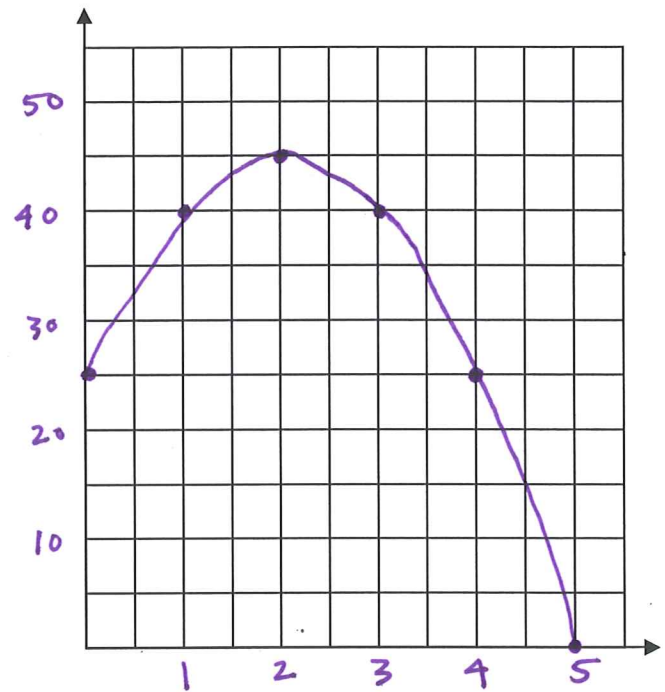
- a. On the grid, sketch a graph of $h(t)$

Show your work on this page.

CANNON BALL!

t	$h(t)$
0	25
1	40
2	45
3	40
4	25
5	0

HEIGHT (m)



TIME (SEC)

3: {

- 1: y-INT @ 0, 25
- 1: VERTEX @ 2, 45
- 1: x-INT @ 5, 0

The questions below refer to the cannonball situation on the previous page.

For each question, be sure to:

- use correct units in your answer
- show your work or explain your reasoning

b. Find $h(1)$. $h(1) = \underline{40}$

Explain the meaning of $h(1)$ in the context of this problem:

AFTER 1 SEC
THE BALL IS 40 m ABOVE THE OCEAN.

c. How high is the cliff above the ocean?

25 m
THIS IS SHOWN BY THE y-INT.

d. Find the maximum height attained by the ball.

45 m.
THIS IS SHOWN IN THE VERTEX

1.5 EACH

 $\left\{ \begin{array}{l} 1: \text{ANS.} \\ \frac{1}{2}: \text{EXPLAIN.} \end{array} \right.$

e. How long does it take for the ball to hit the ocean?

5 SEC.
THIS IS SHOWN IN THE x-INTERCEPT.